# **GLOBAL ACADEMIC RESEARCH INSTITUTE**

COLOMBO, SRI LANKA



# **International Journal of Engineering Science (IJES)**

ISSN 2424-645X

Volume: 01 | Issue: 01

On 15<sup>th</sup> January 2019

http://www.research.lk

Author: Gennady A. Timofeev, Eugene O. Podchasov Bauman Moscow State Technical University, Russia GARI Publisher | Engineering Science | Volume: 01 | Issue: 01 Article ID: IN/GARI/ICET/2018/111 | Pages: 24-30 (07) ISSN 2424-645X | Edit: GARI Editorial Team Received: 23.11.2018 | Publish: 15.01.2019

# BALANCING OF ASYMMETRICAL RHOMBOID MECHANISM OF EXTERNAL HEAT SOURCE ENGINE

<sup>1</sup>Gennady A. Timofeev, <sup>2</sup>Eugene O. Podchasov Department of Robotics and Complex Automation, Bauman Moscow State Technical

> University, Russia Itimga@bmstu.ru, 2podchasov@bmstu.ru

# ABSTRACT

Balancing of asymmetrical rhomboid mechanism with forked crank which is used in engines with external heat sources is considered. The main equations for correcting masses (counterweights) and their coordinates calculations are given. The conditions of full static balancing of rhomboid mechanism with forked crank are obtained.

Key words: external combustion engine, asymmetrical rhomboid mechanism, balancing, correcting masses.

## **INTRODUCTION**

Engines with external sources of heat, also known as external combustion engines, which works with Stirling thermo dynamical cycle have a wide usage with rhomboid mechanisms [1]. That mechanisms are the base ones for machines with shortened thermo dynamical cycle [2-5].

#### LITERATURE REVIEW

Rhomboid mechanisms (fig.1) differs from ordinary crank mechanisms by existence of right and left closed kinematical chain and two pins: working and displacing. Pins chambers connected with each other through cooler and heat

source. Synchronizing gearing allows to eliminate skewness of working and displacing pins. Rhomboid mechanism may be symmetrical or asymmetrical with forked cranks or conrods [2,6,7].

While mechanisms links moves with accelerations force loading of machines basement consists dynamical part. When machine works is steady regime they changes cyclically, forcing periodical loads and causing vibrations of basement. For exclusion or reducing this harmful impact of dynamical loads on engines body, this parts of load should me reduced to zero level, or their amplitudes should be limited in allowable range. Solution of such a problem – balancing of mechanism - is necessary for engine longevity and stable working. Addition of correcting masses in mechanism may lead to zeroing out projections of each links principal vector of inertia forces on each coordinate axis. This means that mechanism will be fully statically balanced.



Figure 1. Generalized scheme of Stirling engine with forked crank.

### **METHODOLOGY**

It is needed to define necessary coordinates of counterweights and their masses. It may be obtained by usage of substitution mass methods, based on replacement of agile links masses by two o three equivalent masses.

Symmetry of rhomboid mechanism relatively pins axis means that the principal moment of inertia forces on OY axis are equal to zero. Projection of the principal moment of inertia forces on OX axis still not equal to zero. (fig. 2) For mechanism with forked crank solution of dynamic reactions balancing problem is



Figure 2. Kinematical chain of rhomboid mechanism of <u>Stirling</u> engine with forked crank:  $1 - forked crank, 2 - working pin's conrod, 3 - working pin, 4 - displacing pin's conrod, 5 - displacing pin; S1, S2, S3 - mass centers of links with masses m1, m2, m3; Rd and <u>Rw</u> - cranks lengths for working and displacing groups, <u>Ld</u> u <u>Lw</u> - lengths of displacing and working conrods, ed u <u>ew</u> - eccentricity of pins, <math>\gamma$  -crank angle.

Distributed masses of mechanisms links replaces by concentrated mass, located in the centers of rotational kinematic pairs. These masses are selected to satisfy the laws of constancy of masses and mass centers location.



Calculation scheme of mechanism (fig. 3) is described by pointed masses with relative abscises in parts of RP.

### DATA ANALYSIS

While working pins crank length is equal to 1 (R=RP=1):

$$\begin{aligned} X_{B} &= \sin \varphi , \qquad (4) \\ X_{D} &= g_{R} \cdot \sin(\varphi - \gamma) \qquad (5) \\ X_{C} &= \sin \varphi - \frac{d_{R} \cdot d_{L}}{\lambda} \cos \varphi_{2} \qquad (6) \\ x_{F} &= a_{R} \left| \sin \left( \varphi - \gamma \right) - \frac{1}{-2} \cos \varphi_{4} \right| \qquad (7) \end{aligned}$$

$$X_{s_1} = \alpha_{s_1} \cdot \sin(\varphi - \varphi_{s_1})$$
(8)

$$X_{x} = a_{x} \cdot \sin(\varphi - \varphi_{x})$$
(9)

where  $a_{i} = \frac{l_{i}}{R}$  - length of  $i_{i}^{\text{th}}$  line segment,  $\lambda_{B}$  - relation

between lengths of displacing conrod to the same crank, while angles  $\phi_2,\,\phi_4$  calculates using equations:

$$\sin \varphi_2 = \frac{\lambda \left[\cos \varphi + \frac{k}{s}\right]}{\left[\frac{a_1}{a_2} + \frac{a_2}{a_3}\right]}$$
(10)
(11)

$$\sin \phi = \lambda \left[ \cos \phi - \gamma + k \right]$$
(11)

where  $k_{\rm B}$  - relative lengths of displacing conrod.

As coordinates (4) – (9) are periodical functions 
$$\int_{1}^{1} (\varphi) = \frac{a_{i}}{\sum_{g \in S} \varphi_{2}}; \int_{2}^{f} (\varphi) = \frac{\cos \varphi_{4}}{\sum_{g}}$$

from  $\phi$  angle with period of  $2\pi$ , they may be expanded in a Fourier series with  $\phi$  as a variable. Functions are even, so coefficient of expansion without sine function are equal to:

$$-1^{1}(())$$

. | Issue: 01 | 15-01-2019

In this case

$$\cos \varphi = \frac{\lambda}{a_{1}} \int_{a_{1}}^{a} A \cos \chi \varphi = \frac{\lambda}{a_{1}} (A + A \cos \varphi + a_{1})$$
(12)

$$\begin{array}{c} +A\cos 2\phi + A\cos \varphi +$$

$$+B_2 \cos 2\varphi + B_3 \cos 3\varphi + B_4 \cos 4\varphi + ...)$$
  
tes (5) (7) through (12) (13) gains (14 14

Expressing the coordinates (5), (7) through (12), (13), gains (14.15)

$$X_{c} = \sin \varphi - a_{\mu} A \cos 2\varphi$$
(14)

$$X_{F} = a_{R} \left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

$$\left| \begin{array}{c} \sin(\varphi - \gamma) - \frac{\pi}{\tau_{*}} B \cos \eta \varphi_{*} \right|$$

To calculate projection of forces on OX axis it is needed to differentiate equations (4), (8), (9), (14) – (15) by time twice and multiple them on masses with opposite sign. This forces equation with R = 1 (for general case of machine movement  $\omega =$  $d\phi/dt = \omega(t)$ ) take the following form:

$$\Phi_{ss} = -\underline{ms} \left( -\omega_2 \cdot \sin \varphi - \varepsilon \cdot \underline{\cos \varphi} \right)$$
<sup>(16)</sup>

$$\Phi_{ss} = -a_{s} m_{D} \left( -\omega_{2} \cdot \sin(\varphi - \gamma) - \varepsilon \cdot \cos(\varphi - \gamma) \right)$$
(17)

$$\Phi_{sc} = -\max_{M_{sc}} \left[ \begin{array}{c} 2 \\ \omega \\ \omega \end{array} \right] - \sin\varphi + \max_{M_{sc}} \sum_{n=0}^{\infty} A_{n} \cos n\varphi + \frac{1}{2} \left[ \begin{array}{c} 2 \\ \omega \\ \omega \end{array} \right]$$
(18)

$$+\varepsilon \left[ -\cos\varphi + a_R \sum_{n=1}^{\infty} A_n \cos \eta \varphi \right]$$

$$\Phi = -a m \left[ 0^{2} \right] - \sin(\varphi - \gamma) + \sum_{n=1}^{\infty} n^{2} A \cos n\varphi$$
(19)

$$+\varepsilon \Big| -\cos(\varphi - \gamma) + \sum_{n=1}^{\infty} uB \cos ua \Big| \Big|$$

$$\Phi_{S_1} = -a_{AS_1} m_1 \left( -\omega_2 \cdot \sin(\varphi - \varphi_{S_1}) - \epsilon \cdot \cos(\varphi - \varphi_{S_1}) \right)$$
(20)

$$\Phi_{SK_1} = -\alpha_{AK_1} m_1 \left( -\omega_2 \cdot \sin(\varphi - \varphi_{SK_1}) - \epsilon \cdot \cos(\varphi - \varphi_{SK_1}) \right)$$
(21)

and others in the same sequence.

The sum of second and higher orders harmonics may be presented in following form:

$$a_{2} \omega^{2} \left[ m_{2} \left[ \frac{a_{2}^{2}}{a_{1}^{2}} a_{2}^{2} \cos n \varphi + m_{2}^{2} \left[ \frac{a_{2}^{2}}{a_{2}^{2}} b_{1}^{2} \cos n \varphi \right] + a_{2} \varepsilon \left[ m_{2} \left[ \frac{a_{1}^{2}}{a_{1}^{2}} a_{2}^{2} \sin n \varphi + m_{F} \sum_{n=2}^{2} \frac{nB_{2}}{nB_{2}} \sin n \varphi \right] = 0$$

$$(22)$$

Solving this equation, gain:

$$\sum_{\substack{n=2\\m m}} \frac{\sum_{n=2}^{n-2} B_n \cos n p}{\sum_{n=1}^{n-2} B_n} = -\frac{m_{c}}{m_{r}} = -C, \qquad (23)$$

$$\sum_{\substack{n=2\\ m \ m \ m}}^{nB_{m}} \sin ng_{m} = \frac{B}{A} = -\frac{m}{m} = -C.$$
(24)

To find the connection of C parameter with engines geometry, formulae (10),

 $\frac{\partial u}{\partial x}\cos\varphi = -\frac{1}{\lambda_{p}}\cos\varphi_{4} + C_{1}\cos\varphi + C_{0}, \text{ is}$ expressed relative with considering cosp.

reduced to the form

$$\cos \varphi = -a \left( C \cos \varphi - C a \sin \varphi \right) + + \lambda C - \frac{C \lambda a k}{a}$$

$$(25)$$

In this equation coefficients with cosp2 and sinp2 considered as values of sine and cosine functions of auxiliary function  $\theta$ :

$$\frac{C}{\rho} = \cos \theta, \quad \frac{C a}{\frac{1}{\rho} R} = \sin \theta,$$

$$\rho = \sqrt{C^2 - \frac{2}{\sqrt{1-R}} a^2} \qquad (26)$$

Equation (25) reduced to the form:

$$\cos \varphi_4 = -z \cos (\varphi_1 + \theta) + z_1 , \qquad (27)$$

where 
$$z = a (\rho, z)$$
  $\left( \begin{array}{c} C_0 - \begin{array}{c} C & a \\ a \end{array} \right)$  (28)

Solving (10) and (11) simultaneously, gains

$$\sin \varphi = \frac{\sin \varphi_{\perp} - \lambda k}{\lambda_{B} \sin \gamma} - \frac{\left(a a \sin \varphi_{\perp} - a \lambda k / a \right)}{\left(\lambda_{B} - \frac{\lambda / a}{\lambda_{B}}\right)}$$
(29)

The expression enclosed in parentheses is denoted by z2 and is expressed through cosp. Using the basic trigonometric identity, expression (29) can be reduced to the form:

$$\frac{\sin^{-2}\varphi_{4} - 2\lambda_{s}k_{s}\sin\varphi_{4} + \lambda_{s}^{2}k_{s}^{2}}{\lambda_{s}^{2}\sin^{-2}\gamma} - \frac{2z(\sin\varphi_{4} - \lambda_{s}^{2})\cot\gamma}{\lambda_{s}\sin\gamma} + \frac{2z(\sin\varphi_{4} - \lambda_{s}^{2})\cot\gamma}{\lambda_{s}\sin\gamma} + \frac{2z(\sin\varphi_{4} - \lambda_{s}^{2})\cos\gamma}{\lambda_{s}\sin\gamma} + \frac{2z(\sin\varphi_{4} - \lambda_{s}^{2})\cos\gamma}{\lambda_{s}\cos\gamma} + \frac{2z(\sin\varphi_{4} - \lambda_{s}^{2})\cos\gamma}{\lambda_{s}\cos\gamma} + \frac{2z(\sin\varphi_{4} - \lambda_{s}^{2})\cos\gamma}{\lambda_{s}\cos\gamma} + \frac{2z(\sin\varphi_{4} - \lambda_{s}^{2})\cos\gamma}{\lambda_{s}\cos\gamma} + \frac{1}{2}$$
(30)

151 Having replaced and introducing new notation, we arrive at the expression:

$$\sin \varphi_4 = \left(\frac{1-z_1}{\frac{2}{\lambda_R} \sin \gamma} + z_5 - 1\right) \frac{1}{\int z_4}, \qquad (31)$$

where:  $z_3 = \cos \varphi 4$ ,

-- ·

$$z_{\downarrow} = \frac{2(k_{g} + z_{2}\cos\gamma)}{\lambda_{B}\sin^{2}\gamma}, z_{\downarrow} = \frac{k_{B}^{2} + 2z_{L}^{2}k_{L}\cos\gamma + z_{L}^{2}}{\sin^{2}\gamma}$$

.

as sin 2 \$\phi\_4 + \cos 2 \$\phi\_4 = 1\$, squaring and folding, one can obtain an identity

$$\begin{array}{l} -z \stackrel{4}{_{3}} + z \stackrel{2}{_{1}} [2(1 + z \stackrel{\lambda}{_{5}} i \sin^{-2}\gamma - \stackrel{\lambda}{_{5}} i \sin^{-2} \gamma - \stackrel{\lambda}{_{5}} i \sin^{-2} \gamma - \stackrel{\lambda}{_{4}} i \sin^{-4} \gamma] - \\ z \stackrel{\lambda}{_{5}} i \stackrel{4}{_{5}} \sin^{-4} \gamma + 2 z (\stackrel{\lambda}{_{5}} i \sin^{-4} \gamma - \stackrel{\lambda}{_{5}} \sin^{-2} \gamma) + \\ 2 \stackrel{\lambda}{_{5}} z \sin^{-2} \gamma - \stackrel{\lambda}{_{5}} i \sin^{-1} \gamma , z \stackrel{2}{_{4}} i \sin^{+} \gamma = 1 \end{array}$$
(32)

When z3, z4, z5 are replaced by their original expressions and, by carrying out the porresponding transformations, we obtain an equivalent identity

$$z_{6} = \frac{a^{1} \cdot a^{2}}{2} + \lambda_{2}^{1} k_{2}^{2} \left( 1 - \frac{2a_{\pi} \cos \gamma}{a_{\pi}} + \frac{a^{2}}{a_{\pi}^{2}} \right),$$

$$z_{1} = 2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{a_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{2\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a_{\pi}} \right),$$

$$I = \frac{\lambda k_{\pi} \left( 1 - \frac{\lambda k_{\pi} \cos \gamma}{a$$

<sup>8</sup> = 2 ar ar cos v.

 $= 2 a \iota a \varsigma \lambda s k s | \cos \gamma - \frac{a}{a \varsigma} |.$ 

From the condition that the values of the amplitudes of the groups of functions  $\cos^4\varphi 2$ ,  $\sin^4\varphi 2$ ;  $\cos^2\varphi 2$ ,  $\sin^2\varphi 2$ ,  $\sin^2\varphi$ 

$$z = a_L a_R$$
 (34)

$$\theta = \gamma$$
 (35)  
 $a_{\mu} = 1$ 

$$a_L \cos \gamma$$
  
 $z = -\lambda k \text{ tg}\theta$  (36)

In which (32) is equal to 1.

It is important to note that conditions (36) - (38) are one of the necessary mechanisms for complete balancing.

Replacing in the formulas from (26) and (28)  $C = \rho \cos\theta$ ,  $z = \alpha \rho$  and using the conditions (34), ( $\rightarrow$ )(35), (36) in the expressions for  $\theta$  and z, we arrive at the relation

Applying this relation in Eq. (23), we obtain one more necessary condition for complete balancing

$$m_c = a_R m_F$$
 (40)

The first-order equation of the sum of all forces has the form

We introduce the following notation:

$$m_{a} + a_{a} m_{a} + m_{c} + a_{a} m_{F} + a_{A} m_{i} \cos \varphi_{S} = m \cos \theta, \qquad (42)$$

$$a_{AS}m \sin \varphi_{S} = m \sin \theta$$
, (43)

$$m^{2} = (m + a m + m + a m_{F} + a_{as1} m \cos \varphi_{s})^{2}$$
(44)

$$(a_{AS}m\sin\varphi_{S})^{2}$$

. .

Then equation (41) takes the form

$$m \sin(\varphi - \theta) = -a_{AR} m \sin(\varphi - \varphi_{SR}),$$
  
(45)

$$m\cos(\varphi-\theta) = -a_{xx}m\cos(\varphi-\varphi_{xx})$$

Solving this system of equations, we find

$$m_{e_{i}} = \frac{m}{a_{x}}$$
(46)

- the value of the correcting mass and the angular coordinate of this mass

$$\varphi_{SK_1} = \pi + \Theta \qquad (47)$$

where

$$\frac{a_{AS} m_1 \sin Q_S}{m_{DC}} m \cos \varphi$$
(48)

#### DISCUSSION

From the results obtained, it follows that (36-38), (40), (45) - (48) are the basic conditions for the complete balancing of the rhombic mechanism of the drive with the forked crank.

## CONCLUSION

The influence of the relations of out-ofaxes, crank radii, lengths of connecting rods, as well as the angle of crank development on the imbalance of the rhombic drive mechanism is determined.

The use of the replacement mass method makes it possible to form, in a convenient form, equations by solving the conditions necessary for the complete balancing of the mechanism.

The symmetry of the considered schemes of mechanisms relative to the axis of motion of the pistons eliminates the effect of inertial forces in the direction perpendicular to this axis and inertial moments.

#### REFERENCES

G.WaLker, Stirling-cycle machines. Calgary: Clarendon Press, 1978

B. Moore, J. Schicho, C. Gosselin, "Dynamic balancing of spherical 4R linkages" Trans. ASME. J. Mech. and Rob. vol. 2, №2, pp. 1-8, 2010.

S. Sayapin "Control system for the Stirling engine", Russian Engineering Research, vol. 37, Issue 10, pp. 841 – 844. 2017.

A. Arbekov, A. Varaksin, A. Inozemtse, "Influence of the by-pass ratio of a basic turbofan engine on the possibility of creating aeroderivative trigeneration power plants" High Temperature Vol. 53, Issue 6, pp. 928-933. 2015.

N. Chainov, L. Myagkov, N. Malastowski, A. Blinov, "Integrated approach for stress analysis of high performance diesel engine cylinder head" IOP Conference Series: Materials Science and Engineering Vol. 327, Issue 5. 2018

M. Basarab, B. Lunin, V. Matveev, E. Chumankin, "Static balancing of metal resonators of cylindrical resonator gyroscopes" Gyroscopy and Navigation Vol. 5 , Issue 4. pp. 213 – 218. 2014.

M. Basarab, B. Lunin, V. Matveev, E. Chumankin. "Balancing of hemispherical resonator gyros by chemical etching" Gyroscopy and Navigation. Vol. 6, Issue 3, pp. 218 - 223. 2015.

nstitute